Neutrinoless double beta decay. What its observation would prove, and its nuclear matrix elements.

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(see also lectures by Prof. Barabash)

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RECOMMENDATION II

The excess of matter over antimatter in the universe is one of the most compelling mysteries in all of science. The observation of neutrinoless double beta decay in nuclei would immediately demonstrate that neutrinos are their own antiparticles and would have profound implications for our understanding of the matterantimatter mystery.

We recommend the timely development and deployment of a U.S.-led ton-scale neutrinoless double beta decay experiment.

A ton-scale instrument designed to search for this as-yet unseen nuclear decay will provide the most powerful test of the particle-antiparticle nature of neutrinos ever performed. With recent experimental breakthroughs pioneered by U.S. physicists and the availability of deep underground laboratories, we are poised to make a major discovery.

How can we tell whether the total lepton number is conserved?

A partial list of processes where the lepton number would be violated:

Neutrinoless $\beta\beta$ decay: $(Z,A) \rightarrow (Z\pm 2,A) + 2e^{(\pm)}, T_{1/2} \rightarrow \sim 10^{26} \gamma$ Muon conversion: $\mu^- + (Z,A) \rightarrow e^+ + (Z-2,A), BR < 10^{-12}$ Anomalous kaon decays: $K^+ \rightarrow \pi^-\mu^+\mu^+$, $BR < 10^{-9}$ Flux of \overline{v}_e from the Sun: BR < 10⁻⁴ Flux of v_e from a nuclear reactor: BR < ? Production at LHC of a pair of the same charge leptons, with no missing energy, through production of doubly charged scalar that decays that way?

Observing any of these processes would mean that the lepton number is not conserved, and that neutrinos are massive Majorana particles.

It turns out that the study of the $0\nu\beta\beta$ decay is by far the most sensitive test of the total lepton number conservation, so we restrict further discussion to this process.

Thanks to the fundamental discoveries of the last two decades we know that neutrino flavor is not conserved. From that it follows that neutrinos are massive and mixed The mass squared differences Δm_{solar}^2 , and $\Delta m_{atmospheric}^2$ have been measured quite accurately, and the three mixing angles (θ_{12} , θ_{23} , θ_{13}) are known as well. However, we do not know the actual absolute neutrino mass, even though we do know that is is quite small, $m_v <$ few eV. That fact, by itself, raises a fundamental question.

We know that ν masses are much much smaller than the masses of other fermions



To solve the dilemma of `unnaturally' small neutrino mass we can give up on renormalizability and add operators of dimension d > 4 that are suppressed by inverse powers of some scale Λ , but are consistent with the SM symmetries.

Weinberg already in 1979 (PLR 43, 1566) showed that there is only one dimension d=5 gauge-invariant operator given the particle content of the standard model:

 $L^{(5)} = C^{(5)}/\Lambda (L^{c} \varepsilon H)(H^{T} \varepsilon L) + h.c.$

Here $L^c = L^T C$, where C is charge conjugation and $\varepsilon = -i\tau_2$. This operator clearly violates the lepton number by two units and represents neutrino Majorana mass

$$L^{(M)} = C^{(5)} / \Lambda v^2 / 2 (\overline{v_L^c} v_L) + h.c.$$

If Λ is larger than v, the Higgs vacuum expectation value, (v= 246 GeV) the neutrinos will be `naturally' lighter than the charged fermions.

All other possible effective operators will be suppressed by higher powers of the energy scale Λ , i.e. Λ^{-n} with n > 2.

The See-Saw (type I) Mechanism was suggested already in ~1980 by Minkowski (1977), Gell-Mann, Ramond, and Slansky(1979), Yanagida(1979), Mohapatra and Senjanovic (1980). It is related to the finding of Weinberg (1979) that there is only one operator of dimension 5 (with only one power of the scale Λ_{LNV} in the denominator). It represents a neutrino Majorana mass realized in the see-saw model.



In the light neutrino exchange, based on the above See-Saw type I, the decay rate is expressed as a product of three factors:

 $1/T_{1/2}^{0\nu} = G^{0\nu}(Q,Z) |M^{0\nu}|^2 |\langle m_{\beta\beta} \rangle|^2$, $\langle m_{\beta\beta} \rangle = |\Sigma_i U_{ei}^2 m_i|$,

which represents a simple relation between the decay rate and the parameters of the neutrino mass matrix.

History of $0\nu\beta\beta$ decay





 $\langle m_{\beta\beta} \rangle$ as a function of the mass of the lightest meutrino. Normal hierarchy in red, inverted hierarchy in green. The reach of the best experiments is indicated by the blue band. The sensitivity of the different tests is indicated in the right panel by the corresponding nuclei. If (or when) the $0\nu\beta\beta$ decay is observed two problems must be still resolved:

a) What is the mechanism of the decay,
i.e., what kind of virtual particle is
exchanged between the affected
nucleons (or quarks)?
b) How to relate the observed decay rate
to the fundamental parameters, i.e.,
what is the value of the corresponding
nuclear matrix elements?

There are two possible, and distinct in physics, but not in their signal signature, mechanisms of $0\nu\beta\beta$ decay. In the following I will concenterate on the simplest light Majorana neutrino exchange. Observation of the $0\nu\beta\beta$ decay will be a signal of ``ew physics" beyond the standard model in all cases.



The long-range, an exchange of a light Majorana neutrino, Neutrino mass is associated with the **See-saw type I** mechanism $m_v \sim v^2/M_N$, where M_N is the very heavy neutrino mass.

The short-range, an exchange of some heavy, often new, particle, it is therefore effectively a contact four nucleon vertex, represented by a dimension 9 operator. The physics of this type of lepton number violation is present in the **see-saw type II** or **type III** models. It is well known that the amplitude for the light neutrino exchange scales as $\langle m_{\beta\beta} \rangle$. On the other hand, if heavy particles of scale Λ are involved the amplitude scales as $1/\Lambda^5$ (dimension 9 operator)

The relative size of the heavy (A_H) vs. light particle (A_L) exchange to the decay amplitude is (a crude estimate, due originaly to Mohapatra)

 $A_{\rm L} \sim G_{\rm F}^2 \, {\rm m}_{\beta\beta}/\langle q^2 \rangle$, $A_{\rm H} \sim G_{\rm F}^2 \, {\rm M}_{\rm W}^4/\Lambda^5$,

where Λ is the heavy scale and $q \sim 100$ MeV is the virtual neutrino momentum.

For $\Lambda \sim 1$ TeV and $m_{\beta\beta} \sim 0.1 - 0.5$ eV $A_L/A_H \sim 1$, hence both mechanisms contribute equally. Thus, the existing $0\nu\beta\beta$ life-time limits constrain Λ_{LNV} to be at least \sim TeV. That scale could be explored e.g. at LHC.

Lets consider briefly the particle physics models in which Onbb-decay of the short-range category might exist. In them LNV violation is associated with low-scale (~TeV) physics, unlike see-saw with LNV at very high scale.

These models include e.g. Left-Right Symmetric Model (LRSM) and RPV SUSY.

Such models contain new, so far unobserved, particles that could be involved in the $0\nu\beta\beta$ decay as well as in the violation of the charged lepton flavor conservation.

Low scale LNV: Left-Right Symmetric Model (LRSM)



The model includes a doubly charged Higgs that couples to leptons as shown

This is an example of $0\nu\beta\beta$ decay mediated by this coupling. The amplitude scales like

$$\frac{g_2^3 \quad h_{ee}}{M_{W_R}^3 M_\Delta^2}$$

Another example is the exchange of heavy right-handed v_R and two W_R that scales like a^4



In both cases the amplitude scales like $1/\Lambda^5$ with $\Lambda \sim M_{W(R)} \sim M_{\Delta} \sim M_{_V(R)}$

Illustration II: RPV SUSY [$R = (-1)^{3(B-L) + 2s}$]

$$W_{RPV} = \lambda_{ijk} L_i L_j E_k^c + \lambda'_{ijk} L_i Q_j D_k^c + \lambda''_{ijk} U_i^c D_j^c D_k^c + \mu'_i L_i H_u$$



The Ovbb amplitude scales as $\frac{\pi\alpha_s \ \lambda_{111}^{\prime 2}}{m_{\bar{g}} \ m_{\bar{f}}^4}$

or in another example as

$$\frac{\pi\alpha_2}{m_{\chi}} \frac{\lambda_{111}^{\prime 2}}{m_{\tilde{f}}^{}}$$

Again with the characteristic $1/\Lambda^5$ scaling

The study of lepton flavor violation (LFV) can help to decide what mechanism is responsible for the $0\nu\beta\beta$ decay if it is observed in a foreseeable future. The models that allow the existence of $0\nu\beta\beta$ decay at $\Lambda_{LNV} \sim 1$ TeV often include an enhancement of LFV as well.

This is based on "Lepton number violation without supersymmetry" Phys.Rev.D 70 (2004) 075007

- V. Cirigliano, A. Kurylov, M.J.Ramsey-Musolf, and P.V.
- and on "Neutrinoless double beta decay and lepton flavor violation" Phys. Rev. Lett. 93 (2004) 231802

V. Cirigliano, A. Kurylov, M.J.Ramsey-Musolf, and P.V.

Lepton flavor violation (LFV) involving charged leptons has not been observed as yet. The most sensitive limits are for the decay

$$B_{\mu \rightarrow e\gamma}$$
 = Γ(μ→eγ)/Γ(μ→eν_μν_e) < 4.2×10⁻¹³

New experiment, MEGII at PSI, aims to reach sensitivity 4×10^{-14} . should reach sensitivity ~ 2 orders of magnitude better.

The "muon conversion" is constrained by

$$\mathsf{B}_{\mu \to e} = \frac{\Gamma(\mu^- + (Z, A) \to e^- + (Z, A))}{\Gamma(\mu^- + (Z, A) \to \nu_{\mu} + (Z - 1, A))} < 6 \times 10^{-13}$$

Several proposals extending the sensitivity to ~10⁻¹⁷ have been proposed.

The fact that neutrinos have finite mass and that they mix will not make these LFV processes observable, they are suppressed by $(\Delta m^2/M_w^2)^2 \le 10^{-50}$. Hence observation of them would imply "new physics" unrelated (or only indirectly related) to neutrino mass.

Summary so far:

- 1) Short-range contributions to the $0\nu\beta\beta$ decay with ~TeV mass scale can lead to the decay rate similar to that of light Majorana neutrino exchange with $\langle m_{\beta\beta} \rangle \sim 0.1 1 \text{ eV}$.
- 2) In order to correctly interpret the experimental results and plan new experiments, it is important to determine the mechanism of the decay. Relation to LFV can help in that respect.
- 3) Next generation of experiments on LFV will extend the sensitivity considerably. In parallel, running of LHC will shed light on the existence of particles with ~TeV masses.

Nuclear Matrix Elements:

In double beta decay two neutrons bound in the ground state of an initial eveneven nucleus are simultaneously transformed into two protons that again are bound in the ground state of the final nucleus.

It is therefore necessary to evaluate, with a sufficient accuracy, **the ground state wave functions of both nuclei**, and evaluate the matrix element of the $0\nu\beta\beta$ -decay operator connecting them.

This cannot be done exactly; some approximation and/or truncation is always needed. Moreover, unfortunately, there is no other analogous observable that can be used to judge the quality of the result.

Can one use the $2\nu\beta\beta$ -decay matrix elements for that? What are the similarities and differences?

Both $2\nu\beta\beta$ and $0\nu\beta\beta$ operators connect the same states. Both change two neutrons into two protons.

However, in $2\nu\beta\beta$ the momentum transfer q < few MeV; thus $e^{iqr} \sim 1$, **long wavelength approximation** is valid, only the GT operator $\sigma\tau$ need to be considered.

In $0\nu\beta\beta$ q ~ 100-200 MeV, $e^{iqr} = 1 + many terms$, there is no natural cutoff in that expansion.

Explaining $2\nu\beta\beta$ -decay rate is necessary but not sufficient

On the other hand since q is high in $0\nu\beta\beta$ the closure approximation is adequate, while in the $2\nu\beta\beta$ we need to sum over all 1⁺ intermediate states in the odd-odd nucleus. **Transition operator** contains $\tau_1^+ \tau_2^+$ that change neutrons into protons plus in the GT part $\sigma_1 \sigma_2$ and in the tensor part operator S_{12} . Each of these parts in multiplied by the `neutrino potential' (Fourier transform of the propagator) that introduces dependence on the radial distance between the nucleons.

$$H(r, E_m) = \frac{R}{2\pi^2} \int \frac{d\vec{q}}{\omega} \frac{1}{\omega + A_m} e^{i\vec{q}\cdot\vec{r}} = \frac{2R}{\pi r} \int_0^\infty dq \frac{q\sin(qr)}{\omega(\omega + A_m)} = \frac{2R}{\pi} \int_0^\infty dq \frac{j_0(qr)q}{q + A_m} \,.$$



fns....nucleon finite size hot...higher order terms in weak currents The radial dependence of M^{0v} ($M^{0v} = \int C(r)dr$) for the indicated nuclei. Only distances r < 2-3 fm contribute, substantially than $R_{nucl.}$ (Identical result obtained in QRPA). Nuclear finite size and short range repulsion need to be included carefully.



Shell model evaluation, Menendez et al., Nucl. Phys. A818, 139 (2009)

Momentum distribution of the contributions to $M^{0\nu}.(M^{0\nu} = \int C(p)dp)$. This example is for ¹³⁶Xe with QRPA. The $p^{2}>^{1/2}$ is 15%-20% larger here than in the nuclear shell model.



Basic procedures: Treat the nucleus as a collection of protons and neutrons bound in a potential well, and interacting through an effective interaction. The procedure consists of several steps:



- Define the valence space
 Derive the effective hamiltonian H_{eff} using the nucleon-nucleon interaction plus some empirical nuclear data.
- Solve the equations of motion to obtain the ground state wave functions

Two complementary procedures are commonly used:

- a) Nuclear shell model (NSM)
- b) Quasiparticle random phase approximation (QRPA)

In NSM a limited valence space is used but all configurations of valence nucleons are included. Describes well properties of low-lying nuclear states. Technically difficult, thus only few $0\nu\beta\beta$ calculations.

In QRPA a **large** valence space is used, but **only a class** of configurations is included. Describes collective states, but not details of dominantly few-particle states. Relatively simple, thus many $0\nu\beta\beta$ calculations.

Calculations of the $0\nu\beta\beta$ nuclear matrix elements were also performed in the Interacting Boson Model (IBM-2) as well as, more recently, using the Energy Density Functional method (or Generator Coordinate Method) that describes in particular quite well the effects related to the nuclear deformation and includes essentially unrestricted valence single particle space.



Why it is difficult to calculate the matrix elements accurately?

Contributions of different angular momenta J of the neutron pair that is transformed in the decay into the proton pair with the same J.

Note the opposite signs, and thus tendency to cancel, between the J = 0 (pairing) and the $J \neq 0$ (ground state correlations) parts.

The same restricted s.p. space is used for QRPA and NSM. There is a reasonable qualitative agreement between the two methods Here is an analogous figure now from the recent application of NSM and for ⁴⁸Ca when two oscillator shells are included (this is so far only possible in this case).

The final values of NME are 0.997 and 1.118 for one or two shells. The short range correlations are not included in this illustration.

Figure from Iwata et al., Phys, Rev. Lett. 116, 112502(2016))





The radial dependence of M^{0v} for the three indicated nuclei. The contributions summed over all components ss shown in the upper panel. The `pairing' J = 0 and `broken pairs' $J \neq 0$ parts are shown separately below. Note that these two parts essentially cancel each other for r > 2-3 fm. This is a generic behavior. Hence the treatment of small values of r and large values of q are quite important.

The finding that the relative distances r < 2-3 fm, and correspondingly that the momentum transfer $q > \sim 100$ MeV means that one needs to consider a number of effects that typically play a minor role in the structure of nuclear ground states:

- a) Short range repulsion
- b) Nucleon finite size
- c) Induced weak currents (Pseudoscalar and weak magnetism)

Each of these, with the present treatment, causes correction (or uncertainty) of ~20% in the $0\nu\beta\beta$ matrix element.

There is a consensus now that these effects must be included and even how they should be treated. Nevertheless, they obviously contribute a substantially uncertainty to the calculated values.

However, if the spread between the matrx element values evaluated using different nuclear models can be treated as a measure of uncertainty, it would dominate the final uncertainty by a big factor.



There are many evaluations of the matrix elements $M^{0\nu}$ using different methods and thus different approximations. It is difficult to conclude which of them is most realistic; each has its strong and weak points.

The spread of the $M^{0\nu}$ values for each nucleus is ~ 3. On the other hand, there is relatively little variation from one nucleus to the next.

In the lower panel the corresponding half-lives for $m_{\beta\beta} = 1$ meV are shown. Obviously, the spread now is ~10, but again, there is no clear

preference for any of the candidate nuclei.

Figure from review by Engel and Menendez

The 2v matrix elements, unlike the 0v ones, exhibit pronounced shell effects. They vary relatively fast as a function of Z or A.



Shell model (black dots) M^{0v} are usually smallest, presumably for two reasons.

- 1) All configurations of valence nucleons are included. Complicated states with high seniority, that are absent in other approaches, further decrease the M^{0v} values.
- 2) Only limited number of orbits can be included. In particular the spin-orbit partners are not included, except in ⁴⁸Ca. Perturbation tests suggest that including additional orbits would increase the M^{0v} values.



The EDF/GCM (Energy Density Functional/Generator Coordinate Method) (blue triangles) gives typically largest M⁰ values. It has several advantages, large s.p. space, realistic treatment of deformation and standard pairing, projection on the correct angular momentum and particle number.

However, it does not include the isoscalar pairing(at least for now), that is known to substantially reduce the $M^{0\nu}$ values.



Illustration of the effect of isoscalar pairing for the GT (largest) part of $M^{0\nu}$. These isotope chains are not real $\beta\beta$ decay candidates, but the calculation shows that the effect is quite general.

From Menendez et al., PRC 93,014305(2016)



The effect of isoscalar pairing is illustrated in The very recent work on GCM for pf shell. The isoscalar pairing was here included and GCM result compared to the exact one. The final NME evaluated In GCM for ⁷⁶Ge and ⁸²Se in this work agree with NSM unlike the earlier results without the isoscalar pairing.

Figure from Jiao et al. arXiv 1707.03940



This work, unlike some of the previous calculations, also is able to reproduce well the experimental occupations of individual orbits. The measurement of occupancies was pioneered by J. P. Schiffer *et al.*, see Phys. Rev. Lett. **100**, 112501, and Phys. Rev. **C79**, 021301. Conclusions from the spread in calculated values:

- 1) It is difficult to decide which of the nuclear models used until now is most realistic.
- 2) We have reasons to believe that the NSM, which gives consistently the smallest values, might be an underestimate.
- 3) In analogy, the EDF approach, which gives the largest values, is very likely an overestimate, at least the versions without the isoscalar pairing.
- 4) However, all model evaluations agree that there is no abrupt change in magnitude from one candidate nucleus to another one. Thus, at least from that point of view, there is no obvious advantage or disadvantage in using any of them.

However, we cannot exclude the possibility that all of the evaluations used so far leave out a common problem that may affect all of them. In fact, the quenching of the axial current matrix elements is an example of such an issue. At this time the most widely discussed source of uncertainty is the ``effective" value of the axial current coupling constant g_A .

From the free neutron β decay the $g_A = 1.27$ is determined. However, it is possible, and there is some evidence, that in the nuclear many-body systems the effective values of g_A is different, and possibly smaller.

The decay rate of the $2\nu\beta\beta$ mode is purely axial vector and thus proportional to g_A^4 . For the $0\nu\beta\beta$ decay, the axial current part is still Dominating, though not pure GT any more. Thus any modification of g_A in heavy nuclei could affect the calculated half-life substantially.

The ISM predictions for the matrix element of several 2ν double beta decays (in MeV⁻¹). See text for the definitions of the valence spaces and interactions.

	$M^{2\nu}(exp)$	q	$M^{2\nu}(th)$	INT
48 Ca $\rightarrow ^{48}$ Ti	0.047 ± 0.003	0.74	0.047	kb3
48 Ca $\rightarrow ^{48}$ Ti	0.047 ± 0.003	0.74	0.048	kb3g
48 Ca \rightarrow 48 Ti	0.047 ± 0.003	0.74	0.065	gxpf1
$^{76}\text{Ge} \rightarrow ^{76}\text{Se}$	0.140 ± 0.005	0.60	0.116	gcn28:50
$^{76}\text{Ge} \rightarrow ^{76}\text{Se}$	0.140 ± 0.005	0.60	0.120	jun45
$^{82}\text{Se} \rightarrow ^{82}\text{Kr}$	0.098 ± 0.004	0.60	0.126	gcn28:50
$^{82}\text{Se} \rightarrow {}^{82}\text{Kr}$	0.098 ± 0.004	0.60	0.124	jun45
128 Te $\rightarrow ^{128}$ Xe	0.049 ± 0.006	0.57	0.059	gcn50:82
130 Te $\rightarrow ^{130}$ Xe	0.034 ± 0.003	0.57	0.043	gcn50:82
136 Xe $\rightarrow ^{136}$ Ba	0.019 ± 0.002	0.45	0.025	gcn50:82

From E. Caurier, F. Nowacki and A. Poves, Phys. Lett. **B711**, 62 (2012)

Since the $2\nu\beta\beta$ decay is simply two GT decays happening at once, the rate is proportional to g_A^2 . Thus, by choosing $g_A^{eff} = q g_A$, with q < 1 so called quenching factor, it is possible to phenomenologically account for any discrepancy.

In M. Horoi and B.A.Brown, arXiv:1301.0256 more single-particle states were included, so that the Ikeda sum rule was obeyed. For ¹³⁶Xe 2v matrix element the M^{2v} = 0.020 MeV⁻¹ was then obtained with quenching q=0.74. So, the inclusion of spin-orbit partners reduces the quenching value to more acceptable values.

In Corraggio et al. (1703.05087) the $2\nu\beta\beta$ decay in ¹³⁰Te and ¹³⁶Xe was treated in a realistic shell model, and q ~ 0.65 was required, less than above.

Quenching of GT matrix elements deduced from the β decay of the sd shell nuclei (A = 17-39). Comparison between the calculated and experimental strength. Typical reduction ~0.77. Other quenching It is remarkable that one parameter is sufficient factors to bring the experiment and theory in agreement $q = g_A^{eff}/g_A$ over a wide region of nuclei. $q = 0.744 \pm 0.015 \, pf$ (from Brown & Wildenthal, Ann.Rev.Nucl. Part.Sci.38,(1988)29) $q = 0.77 \pm 0.02 \, sd$ R(GT) $q = 0.82 \pm 0.02 p$ 1.0 FREE-NUCLEON EFFECTIVE 0.8 EXPERIMENT 0.6 0.4 0.2 0.0 0.6 0.2 0.4 0.8 0.2 0.4 0.60.8 1 0 0 THEORY

Quenching of the axial current operator

When the rate of ordinary β decay is calculated in the nuclear shell model, the corresponding theoretical Gamow-Teller matrix elements are typically larger than their experimental values. Their ratio, however, is nearly constant for a given group of nuclei, when the valence nucleons are in a specified shell.

To account for that effect the quenching factor q < 1 is introduced, that reduces the matrix elements of the GT operator $\sigma\tau$. A convenient way to handle that is to pretend that the coupling g_A is reduced to qxg_A .

Note that the total GT strength, the sum of squares of m.e. over all final states is constrained by the model independent **Ikeda sum rule**

 $S(\beta^{-}) - S(\beta^{+}) = 3(N-Z)$, i.e. $S(\beta^{-}) > 3(N-Z)$

That sum rule is fulfilled in theory if **all** single particle states of an oscillator shell are included in the calculation, including the spin-orbit partners. It is, however, not clear whether the Ikeda sum rule is actually obeyed in real nuclei.

The crucial question: Is the quenching needed in $0\nu\beta\beta$? Are the quenching factors similar to those of $2\nu\beta\beta$?

Since the M_{GT} gives the largest contribution to $M^{0\nu}$, the $0\nu\beta\beta$ rate is approximately proportional to g_A^4 .

Warning: If quenching of q=0.45 is needed, the $\langle m_{\beta\beta} \rangle$ sensitivity is reduced by q² = 0.2, i.e. 5 times.

Remember, in $2\nu\beta\beta$ only intermediate 1⁺ states participate and the momentum transfer q ~ few MeV. In $0\nu\beta\beta$ many multipoles contribute and q ~ 100-200 MeV. So the answer to that question is not straightforward.

What about weak processes with other multipolarities, e.g. forbidden β decays or μ capture? Are they quenched?

Muon capture on nuclei, $\mu^{-} + (Z, A) \rightarrow \nu_{\mu} + (Z-1, A).$

Calculation using RPA (see N. Zinner, K.Langanke and P. Vogel, Phys. Rev. C74, 024326(2006))

This process is dominated by dipole transitions. No quenching is required. In fact, using $g_A = 1.0$ would underestimate the rate by ~0.75.



Matrix elements for unique first forbidden 2⁻ -> 0⁺ β decays in medium mass nuclei. The plotted ratio is M_{exp}/M_{QRPA} for both β^- and β^+ decays.



From Ejiri et al., Phys. Lett. B729, 27 (2014)

Determination of the quenching factor $q = g_A^{eff}/g_A$ from the $2\nu\beta\beta$ decay experimental matrix elements

- 1) In NSM q ~ 0.74 is obtained when the full oscillator shell is included
- 2) In QRPA there is no prediction. The isoscalar interaction constant g_{pp} is adjusted so that the $2\nu\beta\beta$ experimental half-life is obtained.
- 3) In EDF it is impossible, so far, to evaluate the spectrum of 1⁺ states in the virtual intermediate odd-odd nucleus. Thus evaluation of $M^{2\nu}$, without closure, is impossible.
- 4) The same is true in IBM-2. However, the authors, Barea et al., Phys. Rev. C 87, 014315 (2013) argue that the closure approximation might be acceptable and obtain quenching factors that are typically smaller than in ISM, e.g. for ${}^{136}Xe q^{IBM-2} = 0.41$. Note, that this is obtained by assuming that the average energy denominator is $E = 1.12 A^{1/2}$ MeV, roughly the energy of the giant GT resonance. The QRPA and/or NSM do not support this assumption.

One of the suggested explanations of quenching as due to the two-body currents (see Menendez, Gazit, and Schwenk, PRL 107, 062501 (2011)) (This is related to the older ideas of couplings nucleons to the Δ isobars)

Using chiral effective field theory they derive expressions for a significant, and momentum dependent, modification of the axial weak current effective coupling. See also Klos, Menendez, Gazit, and Schwenk PRD **88**, 083516 for more developments of these ideas.



Chiral two-body currents and the 3N force depend on the same couplings. Their values are taken from the previous works.

For a variety of c_3 and c_4 values and $c_D = 0$ the quenching q = 0.66 - 0.85 is obtained for realistic nuclear densities.

Application of chiral two body currents to the evaluation of $M^{0\nu\beta\beta}$ nuclear matrix elements within the QRPA. (Simkovic, Engel, Vogel, Phys.Rev. C89 (2014), 064308)

The 2b currents are included, together with isospin restoration. The resulting $M^{0\nu\beta\beta}$ are reduced by ~20%, while $M^{2\nu\beta\beta}$ are reduced by 66% compared to the unquenched (i.e. one-body currents only) results. The reduction of $M^{0\nu\beta\beta}$ is somewhat less than in the shell model due to the usual g_{pp} adjustment, even though the effect is rather small.



Note the steep dependence of $M^{2\nu\beta\beta}$ on g_{pp} and the mild dependence of $M^{0\nu\beta\beta}$. The values $g_{pp} = 0.897$ and 0.870 are the values that reproduce the experimental $M^{2\nu\beta\beta}$ without and with 2b currents.

Can we make any conclusions regarding g_A quenching?

- 1) Not really. However, all available evidence suggests that the $M^{0\nu}$ evaluated with $g_A = 1.27$, i.e. without quenching, is an overestimate.
- 2) The real issue is whether the matrix elements should be reduced by 20-30% or by a factor of of 3-5. The former would make experiments more difficult but still doable, the latter one would be a game changer.
- 3) Clearly, this is a crucial issue that needs a convincing solution.